Two proposals to transfer some risks related to the carrying of avocado loads

XXIV Jornadas Nacionales y Latinoamericanas Actuariales

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Problem statement

Where does your guacamole come from?



A duck-shaped continent. Source: [3].



The "Place of Fish". Source: [18].



Order vs. Chaos

1. Preparation of soil	6. Transportation to packing facilities		
2. Sowing	7. Emballage		
Adding manure	8. Transportation to export ports		
and fertilizers	or domestic transportation		
4. Irrigation	 Distribution in retail, wholesale stores, and other sale points. 		
5. Harvesting	10. Consumption		

Table 1: Logistics of the production of aguacates.



Distribution of criminal cartels on Michoacán. Source: [1].



Two partial solutions



Hors-route

We use mean-field game theory-like methods to solve a nonzero-sum game on a system of interacting objects and thus propose a method to maximize the market share of the owners of the packing facilities under a long-run criterion.

On the highway

We apply a contingent claims technique to price a financial instrument for funding highway insurance for the transportation of basic materials.



Goals of the research

General goal



Identify affordable methodologies to:

- Compute the fair price of a toll road insurance investment.
- Encourage the competition among packinghouse owners to facilitate access to *aguacatero* orchard owners.



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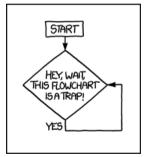


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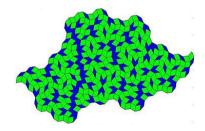
Specific goals.

INEGI

- Isolate algorithms that allow carrying out the valuation of highway insurance.
- Elaborate examples under theoretically accessible hypotheses.



Algorithm obtained from here.



Tessellation obtained from here.



Theoretical framework

Importance of L'or vert du Mexique



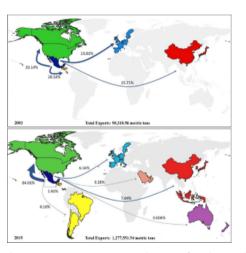


Figure 1: Michoacán is the most important producer of *palta* in the world. Source: [6].

Key facts



According to section 7.3 in [5],

No national program grants credits, nor fiscal incentives to motivate the owners of the packing companies to bring their businesses closer to the producers.

A member of the APEAM, who is also an orchard owner, said

a truck (with 9T of fruit) drives for up to 4h to get to a packing facility from orchards, and none of the 84 *emballage* firms has more than one packing house.

Felony	Cases per 100,000 inhabitants		
Extortion	5050		
Kidnapping	1982		
Car theft	1775		
Robbery	1801		

Table 2: Felonies related to piracy. Source: [19].

The State-of-the-Art

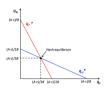




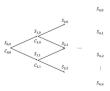
(a) Hotelling's model (see [10]). Image borrowed from here.



(c) Abelian Theorems (see [14]). Image by P. Camargo Bacha.



(b) Cournot's competition (see [11], [13], and [16]). Image borrowed from here.



(d) Contingent claims approach from [8], mixed with simulations from [15]. Image borrowed from here.



Methodology and results

Covering piracy acts hors-route



Figure 3: Location of *Persea Americana* producers, along with **three** packing companies. Borrowed from [12] with information from [2] and [9].



Our protagonists



Initial positions of the players:

- 1. *Empaque Los Reyes S.A. de C.V.* Located at $v_1(0) = (-102.5018, 19.6994)$. (Red marker in figure 3.)
- 2. Avocados Esquivel S. de R.L. Located at $v_2(0)=(-102.4214,19.5266)$. (Blue marker in figure 3.)
- 3. Avoproduce México, S. de P.R. de R.L. de C.V. Located at $v_3(0) = (-101.9380, 19.4136)$. (Orange marker in figure 3.)

This proposal is directed to

the sixth phase referred to in table 1: transportation to packing facilities.

Game rules I



Definition 1

Let S be a finite set, whose members are

(0,v)-Shock due to accident or robbery while going to location v, (1,v)-Client of the first packing company at location v, (2,v)-Client of the second packing company at location v, (3,v)-Client of the third packing company at location v,

where $v \in [-103.216667, -101.783333] \times [18.75, 20.1]$, i.e., v is a point in the rectangle referred to in figure 3.

Remark 1

To ensure S is a finite set, at each time, we allow v to take on only the coordinates of the available packing facilities placed by the central players.

Game rules II



Only one

new packing house by each company.

The status of the n-th orchard at time t = 0, 1, ...

is a random variable $X_n^{35000}(t):\Omega\to S$ defined on the probability space $(\Omega,\mathcal{F},\mathbb{P})$ for n=1,...,35000.

Our central agents will (try to)

control the process $\left(X_n^{35000}(t):t=0,1,...\right)$ for n=1,...,35000. The agents will choose their actions $u_1(t),u_2(t),u_3(t)$ at each time t=0,1,..., from given Borel sets U_1,U_2,U_3 , respectively. For us,

Evolution of the system





(a) Central agents observe market shares $\vec{m}(t) \in \mathbb{P}(S)$. (img: vectorstock.com.)



(c) Agents earn rewards $c_k(\vec{m}, u_1, u_2, u_3)$. Image borrowed from here.



(b) Each agent chooses $u_k = u_k(t) \in U_k$. Image borrowed from here.



(d) System evolves to a new state $\vec{m}' = \vec{M}^{35000}(t+1) \in B$. (img: vectorstock.com.)

The ultimate goal

of the k-th central agent is to maximize

$$J_k^{35000}\left(\pi^{35000}, \vec{m}\right) := \lim_{T \to \infty} \inf \frac{1}{T} \mathbb{E}_{\vec{m}}^{\pi_1^{35000}, \pi_2^{35000}, \pi_3^{35000}} \left[\sum_{t=0}^{T-1} c_k \left(\vec{M}^{35000}(t), u_1(t), u_2(t), u_3(t) \right) \right],$$

where π_ι^{35000} stands for the sequence of actions taken along time by the ι -th player, for $\iota=1,2,3$; and $\mathbb{E}_{\vec{m}}^{\pi_1^{35000},\pi_2^{35000},\pi_3^{35000}}[\cdot]$ is the conditional expectation of $[\cdot]$ given that the central players use the sequence of actions $\left(\pi_1^{35000},\pi_2^{35000},\pi_3^{35000}\right)$, and the distribution of the market share is \vec{m} .



Hotelling-Cournot model without crime



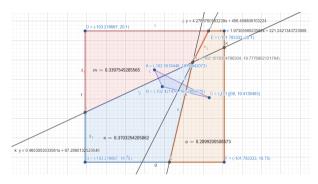


Figure 5: Initial distribution of the market shares *without* considering the pernicious action of crime.

A measure of "bad luck" I



The probability of transition of $X_n^{35000}(\cdot)$ for n=1,2,...,35000 is

$$\mathbb{P}\left(X_n^{35000}(t+1) = j | X_n^{35000}(t) = i, u_1(t) = u_1, u_2(t) = u_2, u_3(t) = u_3\right)
= \int_{\mathbb{R}} \mathbb{I}_j\left(F(i, u_1, u_2, u_3, \xi)\right) \rho(\xi) d\xi.$$

To estimate the density of the random variable ξ ,

we use the information from table 2. The probability that a citizen from Michoacán taken at random suffers at least an extortion, a kidnapping, a car theft, or other sorts of robbery during a year is of $\frac{5050+1982+1775+1801}{100,000}=0.10608$.

A measure of "bad luck" II



Definition 2

Let N be the random variable that counts the number of felonies suffered by a transporter during the year. If further, we assume that N follows Poisson's law, then we have that $\mathbb{P}(N \geq 1) = 0.10608$, which means that

$$\mathbb{P}(N=0) = 0.89392.$$

We use definition 2 to obtain the intensity rate per annum

of $\lambda=0.112138993$ for the felonies suffered by transporters in Michoacán. This number can be used to compute the probability that a transporter gets hijacked during a t-hour period with an Exponential approach: $1-\exp(-\lambda t)$.

A measure of "bad luck" III



Example 3

We readily know that the longest a truck spends on the road is four hours. Then, the estimated probability that they suffer an assault is

$$1 - \exp\left(-0.112138993 \cdot \frac{4}{24 \times 365}\right) = 0.0000512037.$$

Theorem 4

Fix $(u_1,v_1)\in\mathcal{A}$, and let $(x,y)\in\mathcal{A}$. Since the time spent on the road to go from (u,v) to (x,y) is $\frac{4}{1.11157}\sqrt{(x-u)^2+(y-v)^2}$, then the probability of a robbery on \mathcal{A} is $\int_{\mathcal{A}}\int_0^{\frac{4}{1.11157}}\sqrt{(x-u)^2+(u-v)^2}\,1-\mathrm{e}^{-\lambda t}\mathrm{d}t\mathrm{d}\mathcal{A}$.

A measure of "bad luck" in the blue region

By virtue of theorem 4, the proportion of stolen goods in the blue region from figure 5 is:

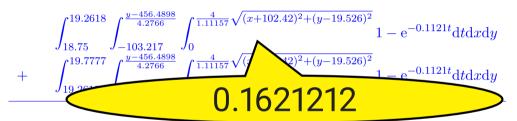
$$+ \int_{19.2618}^{19.2618} \int_{-103.217}^{\frac{y-456.4898}{4.2766}} \int_{0}^{\frac{4}{1.11157}} \sqrt{(x+102.42)^2 + (y-19.526)^2} } 1 - e^{-0.1121t} dt dx dy$$

$$+ \int_{19.2618}^{19.7777} \int_{0.4653}^{\frac{y-456.4898}{4.2766}} \int_{0}^{\frac{4}{1.11157}} \sqrt{(x+102.42)^2 + (y-19.526)^2} } 1 - e^{-0.1121t} dt dx dy$$



A measure of "bad luck" in the blue region

By virtue of theorem 4, the proportion of stolen goods in the blue region from figure 5 is:





A measure of "bad luck" in the red region

By virtue of theorem 4, the proportion of stolen goods in the red region from figure 5 is:

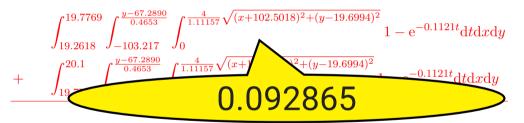
$$\int_{19.7776}^{19.7769} \int_{-0.4653}^{\frac{y-67.2890}{0.4653}} \int_{0}^{\frac{4}{1.11157}} \sqrt{(x+102.5018)^2 + (y-19.6994)^2} 1 - e^{-0.1121t} dt dx dy$$

$$+ \int_{19.7777}^{20.1} \int_{-103.2467}^{\frac{y-67.2890}{0.4653}} \int_{0}^{\frac{4}{1.11157}} \sqrt{(x+102.5018)^2 + (y-19.6994)^2} 1 - e^{-0.1121t} dt dx dy$$



A measure of "bad luck" in the red region

By virtue of theorem 4, the proportion of stolen goods in the red region from figure 5 is:





A measure of "bad luck" in the orange region

By virtue of theorem 4, the proportion of stolen goods in the <u>orange region</u> from figure 5 is:

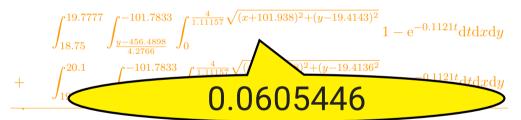
$$\int_{18.75}^{19.7777} \int_{\frac{y-456.4898}{4.2766}}^{-101.7833} \int_{0}^{\frac{4}{1.11157}} \sqrt{(x+101.938)^2 + (y-19.4143)^2} 1 - e^{-0.1121t} dt dx dy$$

$$+ \int_{19.777698}^{20.1} \int_{\frac{y-221.24213}{1.9730556}}^{-101.7833} \int_{0}^{\frac{4}{1.11157}} \sqrt{(x+101.938)^2 + (y-19.4136^2}} 1 - e^{-0.1121t} dt dx dy$$



A measure of "bad luck" in the orange region

By virtue of theorem 4, the proportion of stolen goods in the <u>orange region</u> from figure 5 is:





Setting the board

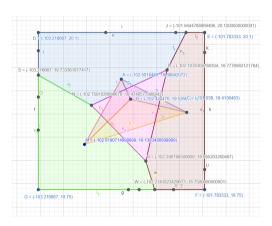
State	Proportion		
$(0, location\ A)$	9.2865%		
$(0, location\ B)$	16.2121%		
$(0, location\ C)$	6.0545%		
$(1, location\ A)$	24.6889%		
$(2, location\ B)$	20.8205%		
$(3, location\ C)$	22.9376%		
Total	100%		

Table 3: Initial distribution of the orchards among the packing facilities and the criminals.



Sequential Hotelling-Cournot model (no crime)

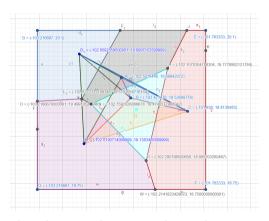




Distribution of the market shares *without* considering the pernicious action of crime after the action of player B.

Sequential Hotelling-Cournot model (no crime)





Distribution of the market shares *without* considering the pernicious action of crime after the action of players B and A.

Sequential Hotelling-Cournot model (no crime)



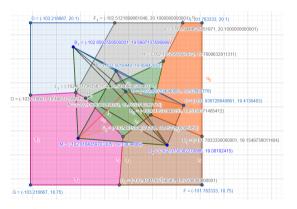


Figure 6: Distribution of the market shares *without* considering the pernicious action of crime after the action of players B, A and C.

Settling the board

Player	Initial market share	Market share at equilibrium	
Empaque Los Reyes	24.6888%	27.9112%	
Avocados Esquivel	20.8205%	33.0206%	
Avopoduce México	22.9376%	28.1823%	
Pirates	31.5531%	10.8859%	
TOTAL	100%	100%	

Comparison of the market shares on table 3, and after the players have exhausted their optimal actions.



A rehabilitated toll road I



From	То	Distance	ADT	Trucks
Pátzcuaro	Huerta Mi Bonita	13.5km	7418	20.9%
Huerta Mi Bonita	Zirahuén	5.5km	6688	18.8%
Zirahuén	Santa Clara del Cobre	12km	11699	24.7%
Santa Clara del Cobre	Jujúcato	7.4km	10322	19.9%
Jujúcato	Ziracuaretiro 1	8.5km	10430	22.9%
Ziracuaretiro 1	Ziracuaretiro 2	4.7km	10220	23.3%
Ziracuaretiro 2	Lazáro Cárdenas	3.1km	18683	20.1%
Lazáro Cárdenas	Uruapan	12.1km	20360	20%

Table 4: Sections of the highway from Pátzcuaro to Uruapan. Source: [7].

A rehabilitated toll road II



Unfortunately, even on these modernized roads, criminals have found ways to affect transporters.

The ADT can help us price hedging instruments against these phenomena in the fashion of [8].

Assumption 1

The highway manager is interested in offering insurance to avocado transporters in case they suffer theft of goods in transit on the highway. To transfer the risk, they would buy coverage from a third party in exchange for a (fair) premium we propose to cover its risk using a correlated variable the ADT.

This proposal is directed to

the eighth phase referred to in table 1: transportation to export ports or domestic transportation.

An attainable earnout

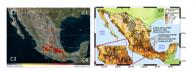




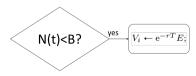
(a) Strict control of ADT. Image derived from here.



(c) Poisson simulation with $\lambda=\mathbb{E}(ADT).$ Image borrowed from here.



(b) The cargo theft and population density maps seem to sustain that a highway with low ADT is more prone to cargo theft. Images borrowed from [17] and [4], respectively.



(d) Binary-like method.

Valuation algorithm



October	0.89415	November	0.96435
December	1.09077	January	0.94472
February	0.86806	March	0.95401
April	1.14642	May	1.00693
Jun	0.97059	July	1.16154
August	1.05416	September	0.94429

Table 5: The seasonal coefficients for the 2023-2024. Source: [8].

$$r = 11.48\%$$
 $B = 20360 \times 20\% = 4072$
 $E = 10^{6}$
 $\lambda = 2546.82$

Algorithm 2: Computation of a 95%-confidence interval for the fair price of the down-and-out option with single arrival of American type

Data: Number of simulations to perform M_i ; time horizon T_i barrier to cross/reach at least one time B_i number of evaluations of the barrier L_i ; monthly daily average volume at the initial time S_0 ; strike price E_i discount rate r; Poisson intensity λ_i : vector of seasonal coefficients R.

Result: 95%-confidence interval for the instrument's value at time t = 0.

```
1 Compute the step size \Delta t \leftarrow \frac{T}{L};

2 for i \leftarrow 1 to M of S o
```

The result



Example 5

We simulate 100,000 times on a one-year horizon and obtain a fair price of 117,693.70 Mexican peso for the instrument, which lies in the 95%-confidence interval [117691.4,117969.01]. Note that our method gives the probability of exercise of this *earnout*. Indeed, taking r=0 and E=1 in our algorithm yields a probability of exercise of 13.39% (cf. [8] for some more details).



The rehabilitated toll road from Pátzcuaro to Uruapan. Source: [18].



Conclusions

Six conclusions I



We present two proposals

oriented to mitigate the risk of suffering losses due to the effect of crime in the Mexican state of Michoacán.

The first is a method to maximize the market share of the owners

of packing houses in the state. We assume that these facilities are located off the existing toll roads. As a by-product of our results, we have shown a way to estimate the probability that the transporters suffer a criminal action on their way toward the packing facilities.

The second proposal is a method to finance an insurance schema

by means of an instrument priced with the aid of the theory of contingent claims. It is oriented to the concessionaires in charge of the management of the highways in the state, and similar companies.

Six conclusions II



Our research is restricted

by the limitations of the two-dimensional view of the geography displayed in figure 3, as it does not consider any geographic accidents, such as rivers, elevations, or depressions. See figure 8, and compare it to figure 6. The difference is notorious.



Figure 8: Actual location of the cities that conform the region DOL_1F_1 in figure 6. Prepared with information from [20].

Six conclusions III



For the sake of illustration,

we have assumed that the distribution of the orchards in the land is uniform, but this hypothesis is not accurate. In the same thread of thought, we have willingly reduced the number of packing companies to only three.

From a theoretical point of view,

an advantage of the examples we presented is that they illustrate a realistic application of our methods.

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¡Diosï meyamu!

Doubts and Suggestions

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